2018 School Competition Sprint Round Problems 1–30

Name

DO NOT BEGIN UNTIL YOU ARE INSTRUCTED TO DO SO.

This section of the competition consists of 30 problems. You will have 40 minutes to complete all the problems. You are not allowed to use calculators, books or other aids during this round. Calculations may be done on scratch paper. All answers must be complete, legible and simplified to lowest terms. Record only final answers in the blanks in the left-hand column of the competition booklet. If you complete the problems before time is called, use the remaining time to check your answers.

In each written round of the competition, the required unit for the answer is included in the answer blank. The plural form of the unit is always used, even if the answer appears to require the singular form of the unit. The unit provided in the answer blank is the only form of the answer that will be accepted.

Total Correct	Scorer's Initials

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	5	Batting	Results
		Result	Number
		Home Run	3
		Triple	1
		Double	2
		Single	<u>2</u>
		Walls	2
		Walk	2
		Out	5
12. percent	A square pen that is surrounded by a fence is dir regions by adding a new fence that connects the sides. By what percent has the total length of fe	vided into two r midpoints of tv ncing been incr	rectangular wo opposite eased?
13	What is the sum of the greatest common factor common multiple of 4 and 18?	of 4 and 18 and	the least
14 years	Claire's three sons, from oldest to youngest, are difference between the ages of Evan and Joel is between the ages of Joel and Alex. If the sum of Joel?	Evan, Joel and the same as the f the three ages	Alex. The difference is 39, how old is
15. <u>mile</u> marker	Danica started her trip at mile marker 66 and en She drove at a constant speed the entire trip. WI by 75% of her trip?	ded her trip at 1 nich mile marke	nile marker 194. er had she reached

16.___

What is the value of $(20 + 12)^2 - (20 - 12)^2$?

17. <u>visitors</u> The table shows the number of visitors over a 4-week period to a new website. What was the average number of visitors to the site per week?

Week	Visitors
1	1028
2	1100
3	1060
4	1056

Website Visitors

18. _____ The Venn diagram shows the number of students at Ramanujan Middle School who play both volleyball and basketball, the number who play one of these sports but not the other, and the number who play neither of these sports. All students at the school are represented in the diagram. What percent of the

students at the school play basketball?



19. ______ Josie selected a number *n*. She divided *n* by 2 and then subtracted $\frac{1}{2}$ from the result. She took half of that result and then subtracted $\frac{1}{2}$ to get the final result of 10. What is the value of *n*?

20. times

Scott repeatedly rolls a pair of standard six-sided dice and keeps track of the sum of the two numbers rolled each time. So far he has not rolled any sum twice. What is the maximum possible number of times he has thrown the dice?

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26. <u>fourth</u> powers	How many of the first one thousand perfect fourth powers have either 1 or 6 as their units digit?
27	Seven jars hold a total of 250 candies. They are lined up left to right from fullest to emptiest. The left-most jar has 72 candies, and the right-most jar has 13. No two jars hold the same number of candies. What is the positive difference between the greatest number of candies that could be in the second jar from the left, and the least number of candies that could be in that jar?
28	What is the greatest integer k such that 2^k is a factor of 67!?
29. <u>nets</u>	How many distinct tetrahedron nets, formed from four connected equilateral triangles, can be cut from the figure shown?
30. triangles	The rows and columns of lattice points in a three-by-three square array are evenly spaced one unit apart. How many distinct triangles with at least one side of length $\sqrt{2}$ units can be drawn using three lattice points for the vertices?

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2018 School Competition Target Round Problems 1 & 2

Name

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This section of the competition consists of eight problems, which will be presented in pairs. Work on one pair of problems will be completed and answers will be collected before the next pair is distributed. The time limit for each pair of problems is six minutes. The first pair of problems is on the other side of this sheet. When told to do so, turn the page over and begin working. This round assumes the use of calculators, and calculations also may be done on scratch paper, but no other aids are allowed. All answers must be complete, legible and simplified to lowest terms. Record only final answers in the blanks in the left-hand column of the problem sheets. If you complete the problems before time is called, use the time remaining to check your answers.

Problem 1	Problem 2	Scorer's Initials

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2018 School Competition Target Round Problems 3 & 4

Name _

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Problem 3	Problem 4	Scorer's Initials

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If *n* is a positive integer such that n^3 is a four-digit number with thousands digit 3. ____ 9, what is the value of *n*? degrees Latoya created this table showing how she spent her time yesterday. She wants 4. to make a pie chart (circle graph) of this data. What is the sum, in degrees, of the central angles of the regions representing the hours she spent at school and the

hours she spent doing homework?

Latoya's Activities

Activity	School	Meals	Homework	Leisure	Sleep	Other
Hours	7	11/2	11/3	11/2	81/2	4 ¹ / ₆

2018 School Competition Target Round Problems 5 & 6

Name ____

DO NOT BEGIN UNTIL YOU ARE INSTRUCTED TO DO SO.

Problem 5	Problem 6	Scorer's Initials

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Three dogs arrived at the dog park at three different times, with their three owners, using three different leash colors. The Dalmatian was next to arrive after the Schnauzer. The dog with the red leash is owned by the 7th grader. The Poodle was not the first to arrive. The Schnauzer does not use a green leash. If the 6th grader owns the Dalmatian, then the Poodle's leash is blue. The 8th grader arrived first. What is the product of the grade levels of the student who arrived second, the student who owns the Poodle and the student who uses the green leash?

5.

6.

Three circles are inscribed in a rectangle of width w and height h as shown. Two of the circles are congruent and are each tangent to two adjacent sides of the rectangle and to each other. The other circle is larger and is tangent to three sides of the rectangle and to the two smaller circles. What the ratio of h to w? Express your answer as a decimal to the nearest hundredth.



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2018 School Competition Target Round Problems 7 & 8

Name _

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Problem 7	Problem 8	Scorer's Initials

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2018 School Competition Team Round Problems 1–10

, Captain

Team	
Members	

DO	NOT	BEGIN	UNTIL	YOU	ARE INSTRUCTED
ΤΟ	DO S	50.			

This section of the competition consists of 10 problems which the team has 20 minutes to complete. Team members may work together in any way to solve the problems. Team members may talk to each other during this section of the competition. This round assumes the use of calculators, and calculations also may be done on scratch paper, but no other aids are allowed. All answers must be complete, legible and simplified to lowest terms. The team captain must record the team's official answers on his/her own competition booklet, which is the only booklet that will be scored. If the team completes the problems before time is called, use the remaining time to check your answers.

Total Correct	Scorer's Initials

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6	There are three integer values of x that make the equation $x^3 + 6x^2 + 11x + 6 = 0$ true. What is the least of these values?
7	A dorm dining hall has three tables. Currently one student is seated at one table, two are seated at another and three are seated at the remaining table. Each student who enters the dining hall picks a table to join with probability proportional to the number of students already seated at the table. Terri enters the dining hall and sits at a table. Ursula then enters the dining hall and sits at a table. What is the probability that there is now a table at which at least four students are seated? Express your answer as a common fraction.
8	A list of numbers of the form $\frac{x}{2}$, for positive integers <i>x</i> , has a sum of 7. What is maximum product of the list of numbers? Express your answer as a common fraction.
9	The figure on the left is a portion of a standard multiplication table that contains the products of all pairs of positive integers. The figure on the right is a contiguous 2-by-2 section of the standard multiplication table, with some digits replaced with question marks. What is the sum of the four numbers in this section? $ \frac{1 2 3 4 5 \cdots}{1 2 3 4 5 \cdots} \\ \frac{1 2 3 4 5 \cdots}{1 2 3 4 5 \cdots} \\ \frac{1 2 3 4 5 \cdots}{1 2 3 4 5 \cdots} \\ \frac{1 2 3 4 5 \cdots}{1 2 3 4 5 \cdots} \\ \frac{1 2 3 4 5 \cdots}{1 2 3 4 5 \cdots} \\ \frac{1 2 3 4 5 \cdots}{1 2 3 4 5 \cdots} \\ \frac{1 2 3 4 5 \cdots}{1 2 3 4 5 \cdots} \\ \frac{1 2 3 4 5 \cdots}{1 2 3 4 5 \cdots} \\ \frac{1 2 3 4 5 \cdots}{1 2 3 4 5 \cdots} \\ \frac{1 2 3 4 5 \cdots}{1 2 3 4 5 \cdots} \\ \frac{1 2 3 4 5 \cdots}{1 2 3 4 5 \cdots} \\ \frac{1 2 3 4 5 \cdots}{1 2 3 4 5 \cdots} \\ \frac{1 2 3 4 5 \cdots}{1 2 3 4 5 \cdots} \\ \frac{1 2 3 4 5 \cdots}{1 2 3 4 5 \cdots} \\ \frac{1 2 3 4 5 \cdots}{1 2 3 4 5 \cdots} \\ \frac{1 2 3 4 5 \cdots}{1 2 3 4 5 \cdots} \\ \frac{1 2 3 4 5 \cdots}{1 2 3 4 5 \cdots} \\ \frac{1 2 3 4 5 \cdots}{1 2 3 4 5 \cdots} \\ \frac{1 2 3 4 5 \cdots}{1 2 3 4 5 \cdots} \\ \frac{1 2 3 4 5 \cdots}{1 3 6 9 12 15 \cdots} \\ \frac{1 2 3 4 5 \cdots}{1 4 8 12 16 20 5 \cdots} \\ \frac{1 2 3 4 5 \cdots}{1 5 20 25 \cdots} \\ \frac{1 3 5 5 10 15 20 25 \cdots}{1 5 10 15 20 25 \cdots} \\ \frac{1 3 5 5 10 15 20 25 \cdots}{1 5 10 15 20 25 \cdots} \\ \frac{1 3 5 5 10 15 20 25 \cdots}{1 5 10 15 20 25 \cdots}{1 10 10 10 10 10 10 10 $
10. <u>ways</u>	Prentice has five daughters and ten identical pens. In how many ways can the pens be distributed among his daughters if two of them, Charlotte and Emily, must get the same number of pens, and every daughter is not required to get a pen?

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